# Package: EpiInvert (via r-universe)

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Type Package

Title Variational Techniques in Epidemiology

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**Description** Using variational techniques we address some epidemiological problems as the incidence curve decomposition by inverting the renewal equation as described in Alvarez et al. (2021) <doi:10.1073/pnas.2105112118> and Alvarez et al. (2022) <doi:10.3390/biology11040540> or the estimation of the functional relationship between epidemiological indicators. We also propose a learning method for the short time forecast of the trend incidence curve as described in Morel et al. (2022) <doi:10.1101/2022.11.05.22281904>.

## URL https://github.com/lalvarezmat/EpiInvert

License GPL (>= 2)

**Encoding** UTF-8

LazyData true

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LinkingTo Rcpp

**Suggests** knitr, ggplot2, grid, dplyr, testthat (>= 3.0.0), rmarkdown, ggpubr

Config/testthat/edition 3

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apply\_delay apply\_delay

## Description

apply a delay vector, s(t), to an indicator, g(t)

## Usage

apply\_delay(g, s)

## Arguments

g	indicator.
S	delay to apply.

## Value

A numeric vector with the result of apply the vector delay s to g.

## Description

EpiIndicators estimates the ratio, r(t), and shift(delay), s(t), between 2 epidemiological indicators f(t) and g(t) following the relation r(t)\*f(t) = g(t+s(t))

## Usage

EpiIndicators(df, config = EpiIndicators\_params())

## Arguments

df	a dataframe with 3 columns: the first column corresponds to the date of each indicator value, the second column is the value of the first indicator f(t) and the third column is the value of the second indicator g(t). A zero value is expected in the case that the real value of an indicator is not available. Indicators must be smooth functions. So, for instance, the raw registered number of cases or deaths are not adequate to run the function. These particular indicators should be smoothed before executing EpiIndicators(), for instance you can use the restored indicator values obtained by EpiInvert()
config	a list of the following optional parameters obtained using the function EpiIndi- cators_params(): s_min = -10,
	• s_min: min value allowed for the shift s(t) (default value -10)
	• s_max: max value allowed for the shift s(t) (default value 25)
	• wr: energy regularization parameter for the ratio r(t) (default value 1000)
	• ws: energy regularization parameter for the shift s(t) (default value 10)
	• s_init: manually fixed initial value (at time t=0) for s(t) (default value -1e6) by default s_init is not fixed and it is automatically estimated
	• s_end: manually fixed final value (at the last time) for s(t) (default value -1e6) by default s_end is not fixed and it is automatically estimated
	• r_init: manually fixed initial value (at time t=0) for r(t) (default value -1e6) by default r_init is not fixed and it is automatically estimated
	• r_end: manually fixed final value (at the last time) for r(t) (default value -1e6) by default r_end is not fixed and it is automatically estimated

## Details

EpiIndicators estimates the ratio, r(t), and shift(delay), s(t) between 2 epidemiological indicators f(t) and g(t) following the relation r(t)\*f(t) = g(t+s(t)) a variational method is proposed to add regularity constraints to the estimates of r(t) and s(t).

#### Value

A dataframe with the following columns :

- date: the date of the indicator values.
- f: the first indicator f(t).
- g: the second indicator g(t).
- r: the estimated ratio r(t)
- s: the estimated shift (delay) s(t)
- f.r: the result of r(t)\*f(t)
- g.s: the result of g(t+s(t))

## Author(s)

Luis Alvarez <lalvarez@ulpgc.es>

#### Examples

```
## load data of epidemiological indicators obtained from the World in data
## organization
data("owid")
## Filter the data to get France epidemiological indicators
library(dplyr)
sel <- filter(owid,iso_code=="FRA")
## Generate a dataframe with the dates and the cases and deaths restored
## using EpiInvert()
df<-data.frame(sel$date,sel$new_cases_restored_EpiInvert,sel$new_deaths_restored_EpiInvert)
## Run EpiIndicators
res <- EpiIndicators(df)</pre>
```

## Plot the results
EpiIndicators\_plot(res)

EpiIndicators\_params EpiIndicators\_params function to select EpiIndicators parameters

#### Description

EpiIndicators\_params function to select EpiIndicators parameters

## Usage

```
EpiIndicators_params(x = "")
```

## EpiIndicators\_plot

## Arguments

x a list with parameters of EpiIndicators() function

#### Value

the EpiIndicators() parameters

#### See Also

EpiIndicators

EpiIndicators\_plot EpiIndicators\_plot

#### Description

EpiIndicators\_plot() plots the results obtained by EpiIndicators()

## Usage

EpiIndicators\_plot(df)

#### Arguments

df

: a dataframe obtained as the outcome of executing EpiIndicators()

## Value

a combination of 3 plots: (A) the indicator f(t) (in green in the main y-axis) and the indicator g(t) (in red in the secondary axis). (B) r(t)\*f(t) (in green in the main y-axis) and g(t+s(t)) (in red in the secondary axis) and (C) r(t) (in green in the main y-axis) and s(t) (in red in the secondary axis)

EpiInvert	EpiInvert estimates the reproduction number Rt and a restored in-
	cidence curve from the original daily incidence curve and the serial
	interval distribution. EpiInvert also corrects the festive and weekly bi-
	ases present in the registered daily incidence.

#### Description

EpiInvert estimates the reproduction number Rt and a restored incidence curve from the original daily incidence curve and the serial interval distribution. EpiInvert also corrects the festive and weekly biases present in the registered daily incidence.

## Usage

```
EpiInvert(
    incid,
    last_incidence_date,
    festive_days = rep("1000-01-01", 2),
    config = EpiInvert::select_params()
)
```

## Arguments

incid	The original daily incidence curve (a numeric vector).		
last_incidence	last_incidence_date		
	The date of the last value of the incidence curve in the format YYYY-MM-DD. EpiInvert does not allow missing values. On days when a country does not report data, a zero must be registered as the value associated with the incidence of that day.		
festive_days	The festive or anomalous dates in the format YYYY-MM-DD (a character vec- tor). In these dates we "a priori" expect that the incidence value is perturbed.		
config	An object of class estimate_R_config, as returned by function select_params. The element of config are :		
	<ul> <li>si_distr: a numeric vector with the distribution of the serial interval (the default value is an empty vector). If this vector is empty, the serial interval is estimated using a parametric shifted log-normal.</li> <li>shift_si_distr: shift of the above user provided serial interval. This shift can be negative, which means that secondary cases can show symptoms before</li> </ul>		
	the primary cases (the default value is 0).		
	• max_time_interval: Maximum number of days used by EpiInvert (the default value is 150, which means that EpiInvert uses the last 150 days. The computational cost strongly depends on this value).		
	• mean_si: mean of the parametric shifted log-normal to approximate the serial interval (in the case the above si_distr vector is empty), (the default value is 12.267893).		
	• sd_si: standard deviation of the parametric shifted log-normal to approxi- mate the serial interval (in the case the above si_distr vector is empty), (the default value is 5.667547).		
	• shift_si=: shift of the parametric shifted log-normal to approximate the se- rial interval (in the case the above si_distr vector is empty), (the default value is -5).		
	• Rt_regularization_weight: regularization weight for Rt in the variational model used by EpiInvert (the default value is 5).		
	• seasonality_regularization_weight: regularization weight for the weekly bias correction factors in the variational model used by EpiInvert (the default value is 5).		
	• incidence_weekly_aggregated: a boolean value which determines if we use weekly aggregated incidence. In such case every week a single data is stored with the accumulated incidence in the last 7 days (the default value is FALSE).		

#### EpiInvert

• NweeksToKeepIncidenceSum: number of weeks to keep the value of the incidence accumulation. The default is 2.

#### Details

EpiInvert estimates the reproduction number Rt and a restored incidence curve by inverting the renewal equation :

$$i(t) = \sum_{k} i(t-k)R(t-k)\Phi(k)$$

using a variational formulation. The theoretical foundations of the method can be found in references [1] and [2].

#### Value

an object of class estimate\_EpiInvert, given by a list with components:

- i\_original: the original daily incidence curve. In the case of weekly aggregated incidence, we initialize the original curve assigning each day of the week 1/7 of the weekly aggregated value.
- i\_festive: the incidence after correction of the festive days bias.
- i\_bias\_free: the incidence after correction of the festive and weekly biases.
- i\_restored: the restored incidence obtained using the renewal equation.
- Rt: the reproduction number Rt obtained by inverting the renewal equation.
- Rt\_CI95: 95% confidence interval radius for the value of Rt taking into account the variation of Rt when more days are added to the estimation.
- · seasonality: the weekly bias correction factors.
- dates: a vector of dates corresponding to the incidence curve.
- festive: boolean associated to each incidence value to check if it has been considered as a festive or anomalous day.
- epsilon: normalized error curve obtained as (i\_bias\_free-i\_restored)/i\_restored^a.
- power\_a: the power, a, which appears in the above expression of the normalized error.
- si\_distr: values of the distribution of the serial interval used in the EpiInvert estimation.
- shift\_si\_distr: shift of the above distribution of the serial interval si\_distr.

#### Author(s)

Luis Alvarez <lalvarez@ulpgc.es>

#### References

[1] Alvarez, L.; Colom, M.; Morel, J.D.; Morel, J.M. Computing the daily reproduction number of COVID-19 by inverting the renewal equation using a variational technique. Proc. Natl. Acad. Sci. USA, 2021.

[2] Alvarez, Luis, Jean-David Morel, and Jean-Michel Morel. "Modeling COVID-19 Incidence by the Renewal Equation after Removal of Administrative Bias and Noise" Biology 11, no. 4: 540. 2022.

[3] Ritchie, H. et al. Coronavirus Pandemic (COVID-19), OurWorldInData.org. Available online: https://ourworldindata.org/coronavirus-source-data (accessed on 5 May 2022).

#### Examples

```
## load data on COVID-19 daily incidence up to 2022-05-05 for France,
## and Germany (taken from the official government data) and for UK and
## the USA taken from reference [3]
data(incidence)
## EpiInvert execution for USA with no festive days specification
## using the incidence 70 days in the past
res <- EpiInvert(incidence$USA,</pre>
"2022-05-05",
"1000-01-01",
select_params(list(max_time_interval = 70))
)
## Plot of the results
EpiInvert_plot(res)
## load data of festive days for France, Germany, UK and the USA
data(festives)
## EpiInvert execution for France with festive days specification using
## 70 days in the past
res <- EpiInvert(incidence$FRA,"2022-05-05",festives$FRA,</pre>
                 select_params(list(max_time_interval = 70)))
## Plot of the incidence between "2022-04-01" and "2022-05-01"
EpiInvert_plot(res,"incid","2022-04-01","2022-05-01")
## load data of a serial interval
data("si_distr_data")
## EpiInvert execution for Germany using the uploaded serial interval shifted
## -2 days, using the incidence 70 days in the past
res <- EpiInvert(incidence$DEU,"2022-05-05",festives$DEU,</pre>
       EpiInvert::select_params(list(si_distr = si_distr_data,
       shift_si_distr=-2,max_time_interval = 70)))
## Plot of the serial interval used (including the shift)
EpiInvert_plot(res, "SI")
```

```
## EpiInvert execution for UK changing the default values of the parametric
## serial interval (using a shifted log-normal) using 70 days in the past
res <- EpiInvert(incidence$UK,"2022-05-05",festives$UK,
        EpiInvert::select_params(list(mean_si = 11,sd_si=6,shift_si=-1,max_time_interval = 70))
        )
## Plot of the reproduction number Rt including an empiric 95\% confidence
## interval of the variation of Rt. To calculate Rt on each day t, EpiInvert
## uses the past days (t'<=t) and the future days (t'>t) when available.
## Therefore, the EpiInvert estimate of Rt varies when there are more days
## available. This confidence interval reflects the expected variation of Rt
## as a function of the number of days after t available.
EpiInvert_plot(res,"R")
```

EpiInvertForecast	EpiInvertForecast computes a 28-day forecast of the restored in- cidence curve including a 95 using the weekly seasonality, from the forecasted restored incidence curve we also estimate a 28-day fore-
	cast of the original incidence curve.

#### Description

EpiInvertForecast computes a 28-day forecast of the restored incidence curve including a 95 using the weekly seasonality, from the forecasted restored incidence curve we also estimate a 28-day forecast of the original incidence curve.

#### Usage

```
EpiInvertForecast(
  EpiInvert_result,
  restored_incidence_database,
  type = "median",
  trend_sentiment = 0,
  NumberForecastAdditionalDays = 0
)
```

#### Arguments

```
EpiInvert_result
```

output list of the EpiInvert execution including, in particular, the restored incidence curve and the seasonality.

```
restored_incidence_database
a database including 27,418 samples of different restored incidence curves com-
puted by EpiInvert using real data. Each restored incidence curve includes the
last 56 values of the sequence. That is this database can be viewed as a matrix
of size 27,418 X 56
type string with the forecast option. It can be "mean" or "median".
```

#### trend\_sentiment

"a priori" knowledge about the future incidence evolution. == 0 means that you are neutral about the future trend > 0 means that you expect that the future trend is higher than the expected one using all database curves. the value represents the percentage of database curves removed before computing the forecast The curves removed are the ones with lowest growth in the last 28 days. < 0 means that you expect that the future trend is higher than the expected one using all database curves. the meaning of the value is similar to the previous case, but removing the curves with the highest growth in the last 28 days.

NumberForecastAdditionalDays

The number of forecast days is 28. With this parameter you can add extra forecast days using linear extrapolation.

#### Details

EpiInvertForecast estimates a forecast of the restored incidence curve using a weighted average of 27,418 restored incidence curves previously estimated by EpiInvert and stored in the database "restored\_incidence\_database". The weight, in the average computation, of each restored incidence curve of the database depends on the similarity between the current curve in the last 28 days and the first 28 days of the database curve. Each database curve contains 56 days. The first 28 days are used for comparison with the current curve and the last 28 days are used for forecasting.

#### Value

a list with components:

- dates: a vector of dates corresponding to the forecast days.
- i\_restored\_forecast: a numeric vector with the forecast of the restored incidence curve for the next 28 days.
- i\_original\_forecast: a numeric vector with the forecast of the original incidence curve for the next 28 days.
- i\_restored\_forecast\_CI50: radius of an empiric confidence interval, with percentile 50, for the restored incidence forecast following the number of days passed since the current day.
- i\_restored\_forecast\_CI75: radius of an empiric confidence interval, with percentile 75, for the restored incidence forecast following the number of days passed since the current day.
- i\_restored\_forecast\_CI90: radius of an empiric confidence interval, with percentile 90, for the restored incidence forecast following the number of days passed since the current day.
- i\_restored\_forecast\_CI95: radius of an empiric confidence interval, with percentile 95, for the restored incidence forecast following the number of days passed since the current day.

#### Author(s)

Luis Alvarez <lalvarez@ulpgc.es>

#### References

[1] Alvarez, L.; Colom, M.; Morel, J.D.; Morel, J.M. Computing the daily reproduction number of COVID-19 by inverting the renewal equation using a variational technique. Proc. Natl. Acad. Sci. USA, 2021.

[2] Alvarez, Luis, Jean-David Morel, and Jean-Michel Morel. "Modeling COVID-19 Incidence by the Renewal Equation after Removal of Administrative Bias and Noise" Biology 11, no. 4: 540. 2022.

[3] Ritchie, H. et al. Coronavirus Pandemic (COVID-19), OurWorldInData.org. Available online: https://ourworldindata.org/coronavirus-source-data (accessed on 5 May 2022).

[4] Alvarez, Luis, Jean-David Morel, and Jean-Michel Morel. EpiInvertForecast Available online: https://ctim.ulpgc.es/covid19/EpiInvertForecastPaper.html

#### Examples

```
## load data on COVID-19 daily incidence up to 2022-05-05 for France,
## and Germany (taken from the official government data) and for UK and
## the USA taken from reference [3]
data(incidence)
## load of the database of restored incidence curves.
data("restored_incidence_database")
## EpiInvert execution for USA with no festive days specification
## using the incidence 90 days in the past
res <- EpiInvert(incidence$USA,
"2022-05-05",
"1000-01-01",
select_params(list(max_time_interval = 90))
)
```

## EpiInvertForecast execution using the EpiInvert results obtained by USA
forecast <- EpiInvertForecast(res,restored\_incidence\_database)</pre>

EpiInvertForecast\_plot

EpiInvertForecast\_plot

## Description

EpiInvertForecast\_plot() plot the restored incidence forecast

#### Usage

EpiInvertForecast\_plot(EpiInvert\_results, Forecast)

## Arguments

EpiInvert_results		
	the list returned by the EpiInvert execution	
Forecast	the list returned by the EpiInvertForecast execution	

## Value

a plot with the last 28 days of the original and restored incidence curves and a 28-day forecast of the same curves. It also includes a shaded area with a 95 of the restored incidence forecast estimation

EpiInvert\_plot EpiInvert\_plot

## Description

EpiInvert\_plot() plots the results obtained by EpiInvert

## Usage

```
EpiInvert_plot(
    x,
    what = "all",
    date_start = "1000-01-01",
    date_end = "3000-01-01"
)
```

## Arguments

х	an object of class estimate_EpiInvert.	
what	one of the following drawing options:	
	• all: a plot combining the main EpiInvert results.	
	• R: a plot of the reproduction number Rt estimation.	
	• incid: a plot combining the obtained incidence curves.	
	• SI: the serial interval used in the EpiInvert estimation.	
date_start	the start date to plot	
date_end	the final date to plot	

## Value

a plot.

## See Also

EpiInvert

festives

## Description

A dataset containing festive days in France, Germany, UK and the USA

#### Usage

festives

## Format

A list with 4 variables:

**FRA** festive day of France

DEU festive day of Germany

**UK** festive day of UK

USA festive day of USA

incidence

A dataset containing daily incidence of COVID-19 for France, Germany, UK and the USA

## Description

A dataset containing daily incidence of COVID-19 for France, Germany, UK and the USA

## Usage

incidence

#### Format

A data frame with 5 variables:

date date of the incidence.

FRA incidence of France.

DEU incidence of Germany.

UK incidence of UK.

USA incidence of USA.

An updated version of this dataset can be found at https://www.ctim.es/covid19/incidence.csv

#### Source

```
https://github.com/owid/covid-19-data/tree/master/public/data
```

https://www.santepubliquefrance.fr/dossiers/coronavirus-covid-19/coronavirus-chiffres-cles-et-evolution-covid-19/coronavirus-chiffres-cles-et-evolution-covid-19/coronavirus-chiffres-cles-et-evolution-covid-19/coronavirus-chiffres-cles-et-evolution-covid-19/coronavirus-chiffres-cles-et-evolution-covid-19/coronavirus-chiffres-cles-et-evolution-covid-19/coronavirus-chiffres-cles-et-evolution-covid-19/coronavirus-chiffres-cles-et-evolution-covid-19/coronavirus-chiffres-cles-et-evolution-covid-19/coronavirus-chiffres-cles-et-evolution-covid-19/coronavirus-chiffres-cles-et-evolution-covid-19/coronavirus-chiffres-cles-et-evolution-covid-19/coronavirus-chiffres-cles-et-evolution-covid-19/coronavirus-chiffres-cles-et-evolution-covid-19/coronavirus-chiffres-cles-et-evolution-covid-19/coronavirus-chiffres-cles-et-evolution-covid-19/coronavirus-chiffres-cles-et-evolution-covid-19/coronavirus-chiffres-cles-et-evolution-covid-19/coronavirus-chiffres-cles-et-evolution-covid-19/covid

https://experience.arcgis.com/experience/478220a4c454480e823b17327b2bf1d4/page/page\_
1/

incidence\_weekly\_aggregated

A dataset containing weekly aggregated incidence of COVID-19 for France, Germany, UK and the USA

#### Description

A dataset containing weekly aggregated incidence of COVID-19 for France, Germany, UK and the USA

## Usage

incidence\_weekly\_aggregated

#### Format

A data frame with 5 variables:

date date of the weekly aggregated incidence.

FRA weekly aggregated incidence of France.

DEU weekly aggregated incidence of Germany.

UK weekly aggregated incidence of UK.

USA weekly aggregated incidence of USA.

An updated version of this dataset can be found at https://www.ctim.es/covid19/incidence.csv

#### Source

https://github.com/owid/covid-19-data/tree/master/public/data https://www.santepubliquefrance.fr/dossiers/coronavirus-covid-19/coronavirus-chiffres-cles-et-evolu https://experience.arcgis.com/experience/478220a4c454480e823b17327b2bf1d4/page/page\_ 1/

joint\_indicators\_by\_date

joint\_indicators\_by\_date

#### Description

generates a dataframe joining the dates and values of 2 indicators

## Usage

```
joint_indicators_by_date(date0, i0, date1, i1)
```

#### Arguments

date0	the dates of the first indicator.
iØ	the values of the first indicator.
date1	the dates of the second indicator.
i1	the values of the second indicator.

## Value

A dataframe with the following columns :

- date: all dates presented in any of the indicators.
- f: the values of the first indicator. We assign 0 in the case the data is not available for a given day.
- g: the values of the second indicator. We assign 0 in the case the data is not available for a given day

owid

A dataset with COVID-19 indicators

## Description

A dataset containing COVID-19 epidemiological indicators for Canada, France, Germany, Italy, UK and the USA from Our World in data organization https://github.com/owid/covid-19-data/tree/master/public/data up to 2022-11-28. In the case a data value is not available for a given day we assign the value 0 to the indicator

#### Usage

owid

#### Format

A dataframe with 13 variables:

iso\_code iso code of the country

location country name

date date of the indicator value

new\_cases new confirmed cases

new\_cases\_smoothed new confirmed cases smoothed

new\_cases\_restored\_EpiInvert new confirmed cases restored using EpiInvert

new\_deaths new deaths attributed to COVID-19

new\_deaths\_smoothed new deaths smoothed

new\_deaths\_restored\_EpiInvert new deaths restored using EpiInvert

icu\_patients number of COVID-19 patients in intensive care units (ICUs) on a given day

hosp\_patients number of COVID-19 patients in hospital on a given day

- weekly\_icu\_admissions number of COVID-19 patients newly admitted to intensive care units (ICUs) in a given week (reporting date and the preceding 6 days)
- **weekly\_hosp\_admissions** number of COVID-19 patients newly admitted to hospitals in a given week (reporting date and the preceding 6 days)

restored\_incidence\_database

A dataset of restored daily incidence trend curves

## Description

A dataset including 27,418 samples of different restored incidence curves computed by EpiInvert using real data. Each restored incidence curve includes the last 56 values of the sequence.

#### Usage

restored\_incidence\_database

#### Format

A 27,418 X 56 numeric matrix

select\_params

## Description

select\_params function to select EpiInvert parameters

#### Usage

select\_params(x = "")

## Arguments

#### х

a list with elements of the class estimate\_R\_config

#### Value

an object of class estimate\_R\_config.

## See Also

EpiInvert

si\_distr\_data A dataset containing the values of a serial interval

## Description

A dataset containing the values of a serial interval

## Usage

si\_distr\_data

## Format

A numeric vector with 1 variable representing the serial interval

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